

Computer Organization and Structure

Homework #1
Due: 2004/10/12

1. Given the following three functions:

- I. A 2-bit-wide *shifter* takes two input signals, i_0 and i_1 , and shifts them to two outputs, o_0 and o_1 , under the control of a shift signal. If this signal SHIFT is false, then the inputs are connected straight through to the outputs. If SHIFT is true, then i_0 is routed to o_1 and o_0 should be set to a 0.
- II. A 1-bit *demultiplexer* takes an input signal IN and shifts it to one of two outputs, o_0 and o_1 , under the control of a single SELECT signal. If SELECT is 0, then IN is connected through to o_0 and o_1 is connected to a 0. If SELECT is 1, then IN is connected through to o_1 and o_0 is connected to a 0.
- III. A 2-bit *multiplexer* takes two input signals, i_0 and i_1 , and shifts one of them to the single output OUT under the control of a 1-bit select signal. If the SELECT signal is false, then i_0 is passed to OUT. If SELECT is true, then i_1 is passed to OUT.

- a. Write truth tables.
- b. Write sum of products expressions.
- c. Draw logic schematics using AND, OR, and INVERT gates.

2. Draw schematics for the following functions in terms of AND, OR, and inverter gates.

- a. $X(Y + Z)$
- b. $XY + XZ$
- c. $\overline{X(Y + Z)}$
- d. $\overline{X} + \overline{YZ}$
- e. $W(X + YZ)$

3. Draw the schematics for the following functions using NOR gates and inverters only:

- a. $\overline{\overline{\overline{X + (Y + Z)}}}$
- b. $\overline{\overline{(\overline{X + Y}) + (\overline{X + Z})}}$

4. Prove the following simplification theorems using the first eight laws of Boolean algebra:

- a. $(X + Y)(X + \overline{Y}) = X$
- b. $X(X + Y) = X$
- c. $(X + \overline{Y})Y = XY$

d. $(X + Y)(\bar{X} + Z) = XZ + \bar{X}Y$

5. Simplify the following functions using the theorems of Boolean algebra. Write the particular law or theorem you are using in each step. For each simplified function you derive, how many literals does it have?
- $f(X, Y) = XY + X\bar{Y}$
 - $f(X, Y) = (X + Y)(X + \bar{Y})$
 - $f(X, Y, Z) = Y\bar{Z} + \bar{X}YZ + XYZ$
 - $f(X, Y, Z) = (X + Y)(\bar{X} + Y + Z)(\bar{X} + Y + \bar{Z})$
 - $f(W, X, Y, Z) = X + XYZ + \bar{X}YZ + \bar{X}Y + WX + \bar{W}X$
6. Consider a four-input Boolean function that is asserted whenever exactly two of its inputs are asserted.
- Construct its truth table.
 - What is the function in sum of products form, using “little m ” notation?
 - What is the function in product of sums form, using “big M ” notation?
 - Use the Karnaugh map method to simplify the function in sum of products form.